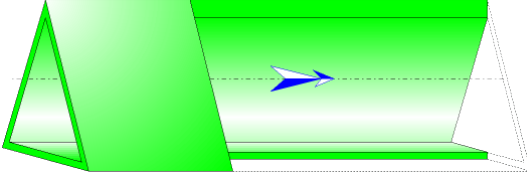




Straight Pipe Triangular Cross-Section and Roughness Walls (MILLER)



Model description:

This model of component calculates the major head loss (pressure drop) of a horizontal straight pipe of triangular and constant cross-section. In addition, the flow is assumed fully developed and stabilized.

The head loss is due to the friction of the fluid on the inner walls of the piping and is calculated with the Darcy formula.

Darcy friction factor is determined:

- for laminar flow regime by the law of Hagen-Poiseuille (independent of the value of relative roughness),
- for turbulent flow regime by the explicit Swamee-Jain equation (dependent of the value of relative roughness), the explicit Swamee-Jain equation is a Colebrook-White equation approximation,
- for critical flow regime by interpolation between friction factors of laminar and turbulent flow.

Model formulation:

Top angle (°):

$$\theta = 2 \cdot \tan^{-1} \left(\frac{w}{2 \cdot h} \right)$$

Hydraulic diameter (m):

$$D = \frac{2 \cdot h}{1 + \sqrt{\tan^2 \left(\frac{\theta}{2} \right) + 1}}$$

Cross-section area (m²):

$$A = \frac{w}{2} \cdot h$$

Mean velocity (m/s):

$$U = \frac{Q}{A}$$

Mass flow rate (kg/s):

$$m = Q \cdot \rho$$

Fluid volume in the pipe (m³):

$$V = A \cdot L$$

Fluid mass in the pipe (kg):

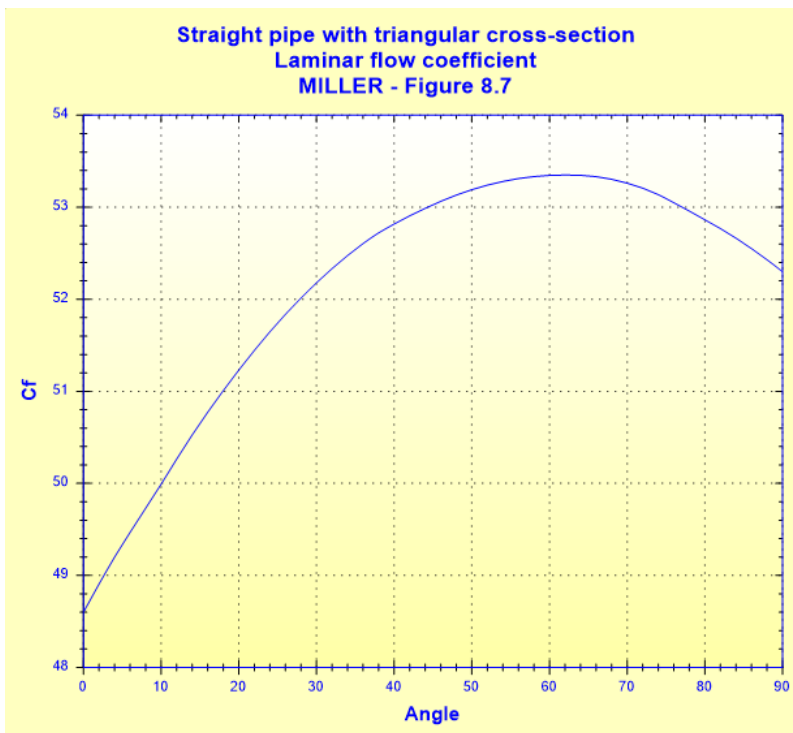
$$M = V \cdot \rho$$

Reynolds number:

$$Re = \frac{U \cdot D}{\nu}$$

Laminar flow coefficient:

$$Cf = f(\theta) \quad ([1] \text{ figure 8.7})$$

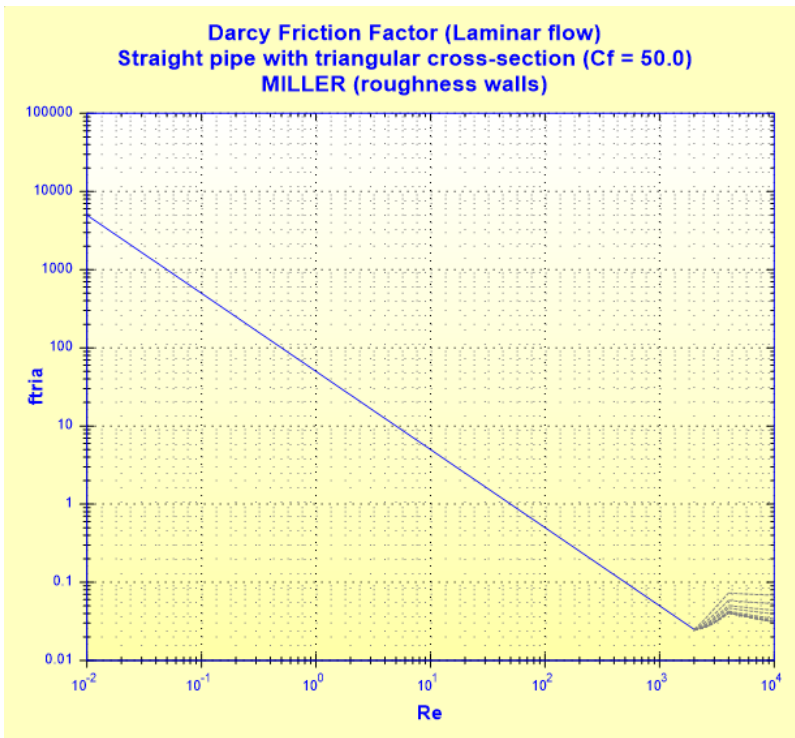


Darcy friction factor:

- laminar flow regime ($Re \leq 2000$):

Darcy friction factor for triangular cross-section:

$$f_{tria} = \frac{Cf}{Re} \quad ([1] \text{ equation 8.7})$$



([1] equation 8.7 with $C_f =$

50)

■ turbulent flow regime - transition region and complete turbulence region ($Re \geq 4000$):

Darcy friction factor for circular cross-section:

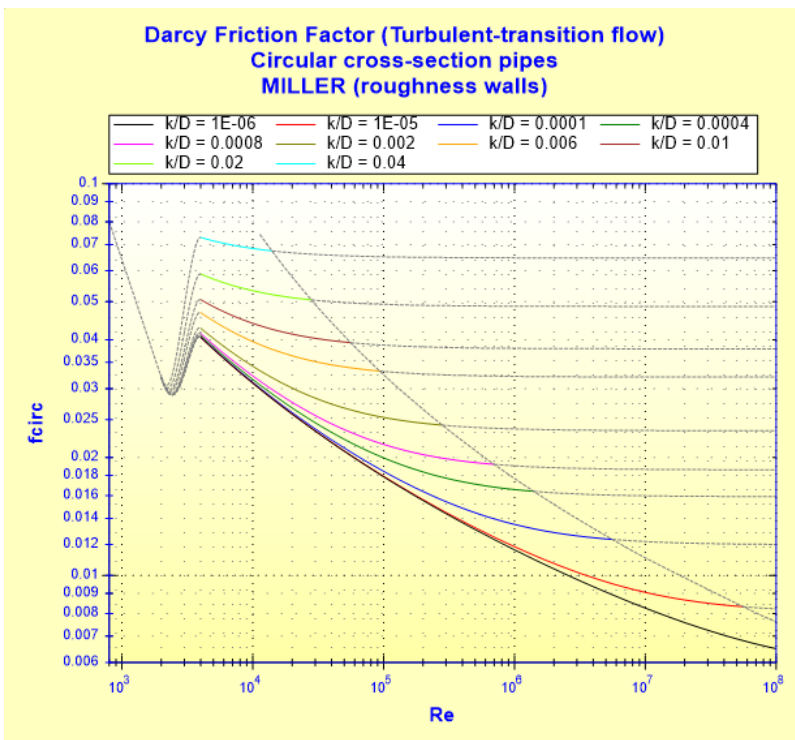
Swamee-Jain equation (Colebrook-White equation approximation)

$$f_{circ} = \frac{0.25}{\left[\log \left(\frac{k}{3.7 \cdot D} + \frac{5.74}{Re^{0.9}} \right) \right]^2} \quad ([1] \text{ equation 8.4})$$

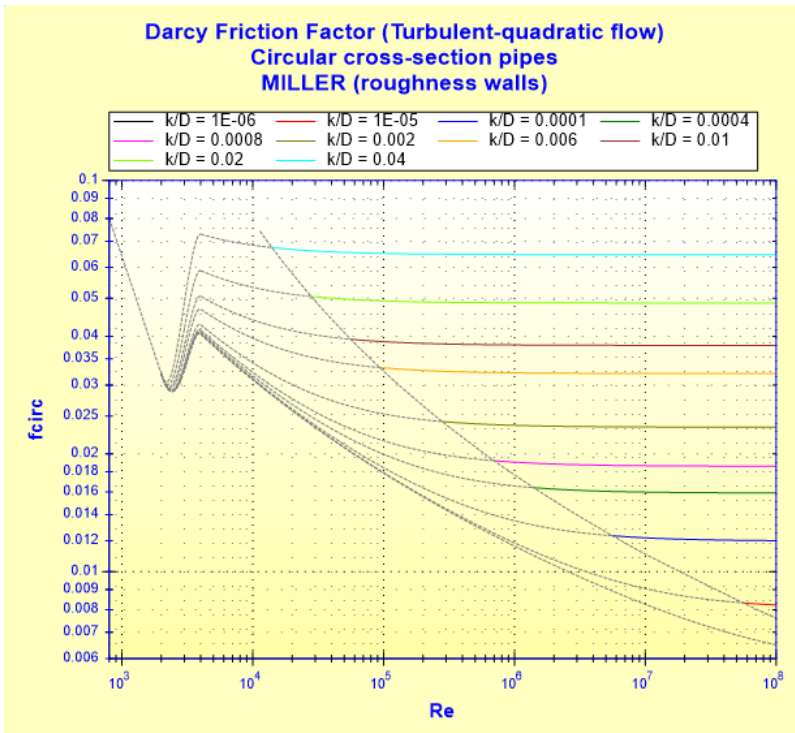
Reynolds number corresponding to the beginning of complete turbulence:

$$Re''_{lim} = \frac{560}{k/D} \quad ([2] \text{ diagram 2.4})$$

Transition region



Complete turbulence region



Darcy friction factor for triangular cross-section:

$$f_{tria} = f_{circ}$$

- critical flow regime ($2000 < Re < 4000$):

Darcy friction factor for circular cross-section:

cubic interpolation

$$f_{circ} = (X1 + R \cdot (X2 + R \cdot (X3 + X4))) \quad ([3])$$

with:

$$R = \frac{Re}{2000}$$

$$X1 = 7 \cdot FA - FB$$

$$X2 = 0.128 - 17 \cdot FA + 2.5 \cdot FB$$

$$X3 = -0.128 + 13 \cdot FA - 2 \cdot FB$$

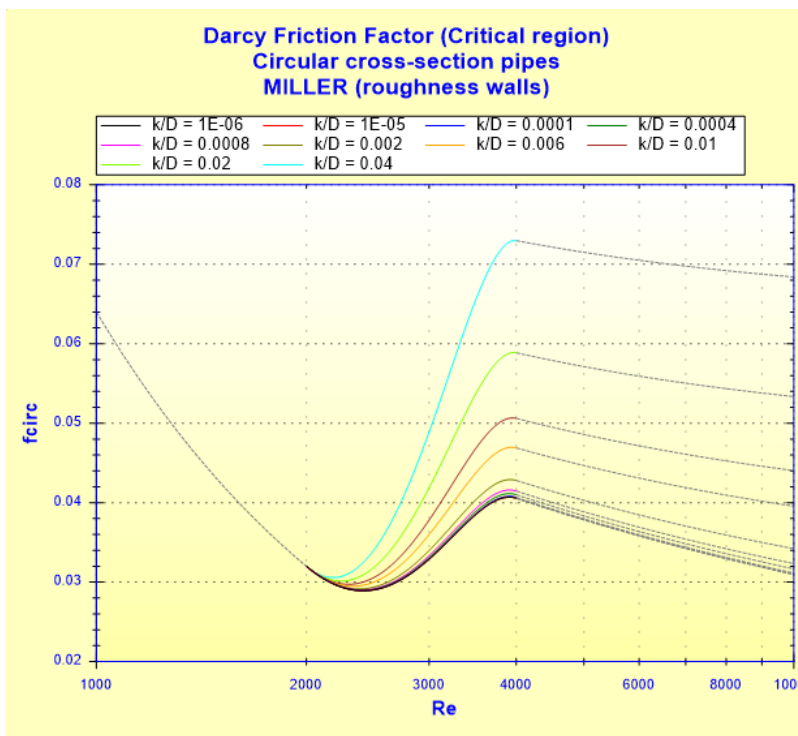
$$X4 = R \cdot (0.032 - 3 \cdot FA + 0.5 \cdot FB)$$

$$FA = Y3^{-2}$$

$$FB = FA \cdot \left(2 - \frac{0.00514215}{Y2 \cdot Y3} \right)$$

$$Y2 = \frac{k}{3.7 \cdot D} + \frac{5.74}{Re^{0.9}}$$

$$Y3 = -0.86859 \cdot \ln \left(\frac{k}{3.7 \cdot D} + \frac{5.74}{4000^{0.9}} \right)$$



Darcy friction factor for triangular cross-section:

$$f_{tria} = f_{circ}$$

Friction pressure loss coefficient:

$$K_f = f_{tria} \cdot \frac{L}{D} \quad ([1] \text{ equation 8.3})$$

Total pressure loss coefficient (based on the mean pipe velocity):

$$K = K_f$$

Total pressure loss (Pa):

$$\Delta P = K \cdot \frac{\rho \cdot U^2}{2} \quad ([1] \text{ equation 8.1b})$$

Total head loss of fluid (m):

$$\Delta H = K \cdot \frac{U^2}{2 \cdot g} \quad ([1] \text{ equation 8.1a})$$

Hydraulic power loss (W):

$$Wh = \Delta P \cdot Q$$

Symbols, Definitions, SI Units:

w	Cross-section base (m)
h	Cross-section height(m)
θ	Top angle ($^{\circ}$)
D	Hydraulic diameter (m)
A	Cross-section area (m^2)
Q	Volume flow rate (m^3/s)
U	Mean velocity (m/s)
m	Mass flow rate (kg/s)
L	Pipe length (m)
V	Fluid volume in the pipe (m^3)
M	Fluid mass in the pipe (kg)
Re	Reynolds number ()
Cf	Laminar flow coefficient ()
k	Absolute roughness of walls (m)
f_{circ}	Darcy friction factor for circular cross-section ()
Re''_{lim}	Reynolds number corresponding to the beginning of complete turbulence ()
f_{tria}	Darcy friction factor for triangular cross-section ()
K_f	Friction pressure loss coefficient ()
K	Total pressure loss coefficient (based on the mean pipe velocity) ()
ΔP	Total pressure loss (Pa)
ΔH	Total head loss of fluid (m)
Wh	Hydraulic power loss (W)
ρ	Fluid density (kg/m^3)
ν	Fluid kinematic viscosity (m^2/s)
g	Gravitational acceleration (m/s^2)

Validity range:

- any flow regime: laminar, critical and turbulent ($Re \leq 10^8$)
- relative roughness $k/D \leq 0.05$
- stabilized flow

Example of application:

HydrauCalc 2019b - [Straight pipe triangular cross-section and roughness walls - MILLER (2nd Ed.)]

File Edit Preferences Calculation method Database Tools Help

Fluid characteristics
 Fluid: Water @ 1 atm [HC]
 Ref.: IAPWS IF97
 Temperature: T 20 °C
 Pressure: P 1.013 bar
 Density: ρ 998.2061 kg/m³
 Dynamic Viscosity: μ 0.00100159 N.s/m²
 Kinematic Viscosity: ν 1.00340E-06 m²/s
 Density Dyn. Visc. Kn. Visc.

Geometrical characteristics
 Help Info Moody Chart Calculate

 Pressure loss ΔP 0.009553567 bar
 ΔH 0.0976 m of fluid

Complementary results

Designation	Symbol	Value	Unit
Hydraulic diameter	D	0.04142136	m
Top angle	θ	90	°
Pipe cross-section area	A	0.0025	m ²
Internal pipe volume	V	0.0025	m ³
Mass of fluid in the pipe	M	2.495515	kg
Relative roughness	k/D	0.0002414213	
Reynolds number	Re	82562.24	
<input checked="" type="checkbox"/> Friction factor for circular cross-section	f _{circ}	0.01982165	
Darcy Friction Factor for triangular cross-section	f _{tria}	0.01982165	
Pressure loss per length unit		0.009553567	bar/m
Pressure loss coefficient (based on the mean pipe velocity)	K	0.4785369	
Hydraulic power loss	Wh	4.776783	W

References:

- [1] Internal Flow System, Second Edition, D.S. Miller (1990)
- [2] Handbook of Hydraulic Resistance, 3rd Edition, I.E. Idelchik (2008)
- [3] Dunlop (1991)