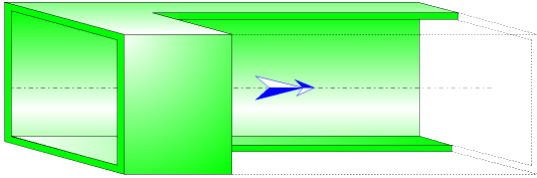




Straight Pipe Rectangular Cross-Section and Uniform Roughness Walls (IDELCHIK)



Model description:

This model of component calculates the major head loss (pressure drop) of a horizontal straight pipe of square or rectangular and constant cross-section. In addition, the flow is assumed fully developed and stabilized.

The head loss is due to the friction of the fluid on the inner walls of the piping and is calculated with the Darcy formula. The roughness of the inner walls of the pipe is supposed uniform (pipe used by Nikuradse for its experimental data).

Darcy friction factor is determined:

- for laminar flow regime by the law of Hagen-Poiseuille (independent of the value of relative roughness),
- for turbulent flow regime by the Nikuradse equation (dependent of the value of relative roughness),
- for critical flow regime by interpolation between friction factors of laminar and turbulent flow.

Model formulation:

Hydraulic diameter (m):

$$D_h = \frac{2 \cdot a_0 \cdot b_0}{a_0 + b_0} \quad ([1] \text{ diagram 2.6})$$

Cross-section area (m²):

$$F_0 = a_0 \cdot b_0$$

Mean velocity (m/s):

$$w_0 = \frac{Q}{F_0}$$

Mass flow rate (kg/s):

$$G = Q \cdot \rho$$

Fluid volume in the pipe (m³):

$$V = F_0 \cdot l$$

Fluid mass in the pipe (kg):

$$M = V \cdot \rho$$

Reynolds number:

$$Re = \frac{w_0 \cdot D_h}{\nu}$$

Relative roughness:

$$\bar{\Delta} = \frac{\Delta}{D_h}$$

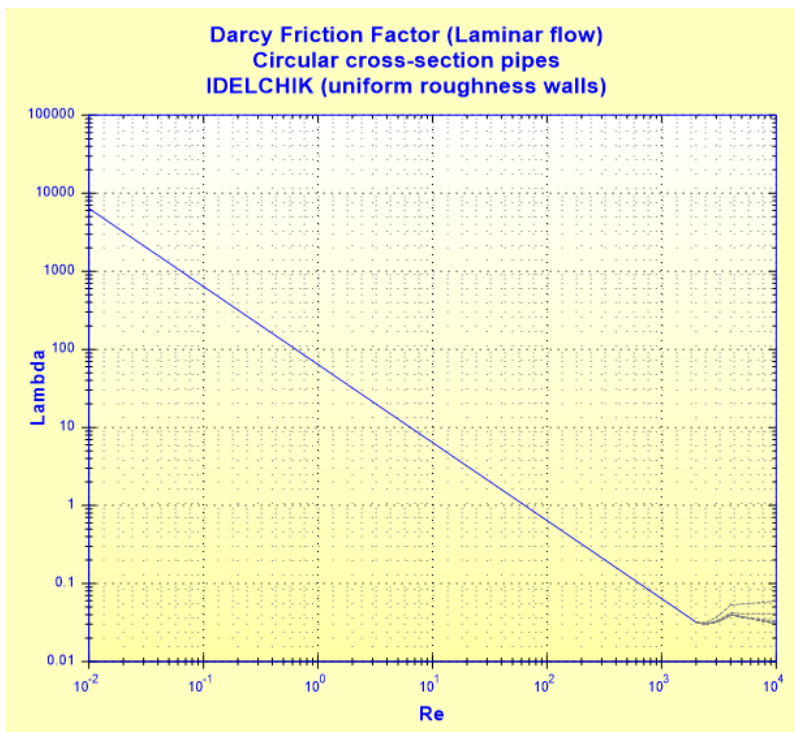
Darcy friction factor for circular cross-section:

- laminar flow regime ($Re \leq 2000$):

Hagen-Poiseuille law

$$\lambda = \frac{64}{Re}$$

([1] diagram 2.1)



- turbulent flow regime - transition region and complete turbulence region ($Re \geq 4000$):

Nikuradze equation

$$\lambda = \frac{1}{\left[a_1 + b_1 \cdot \log(\text{Re} \cdot \sqrt{\lambda}) + c_1 \cdot \log(\bar{\Delta}) \right]^2}$$

([1] diagram 2.2)

where the values of a_1 , b_1 and c_1 are given below:

$\bar{\Delta} \cdot \text{Re} \cdot \sqrt{\lambda}$	a_1	b_1	c_1
3.6 - 10	-0.800	2.000	0.000
10 - 20	0.068	1.130	-0.870
20 - 40	1.538	0.000	-2.000
40 - 191.2	2.471	-0.588	-2.588
> 191.2	1.138	0.000	-2.000

Reynolds number at which pipe cease to be hydraulically smooth:

$$\text{Re}'_{\text{lim}} = \frac{26.9}{\bar{\Delta}^{-1.143}}$$

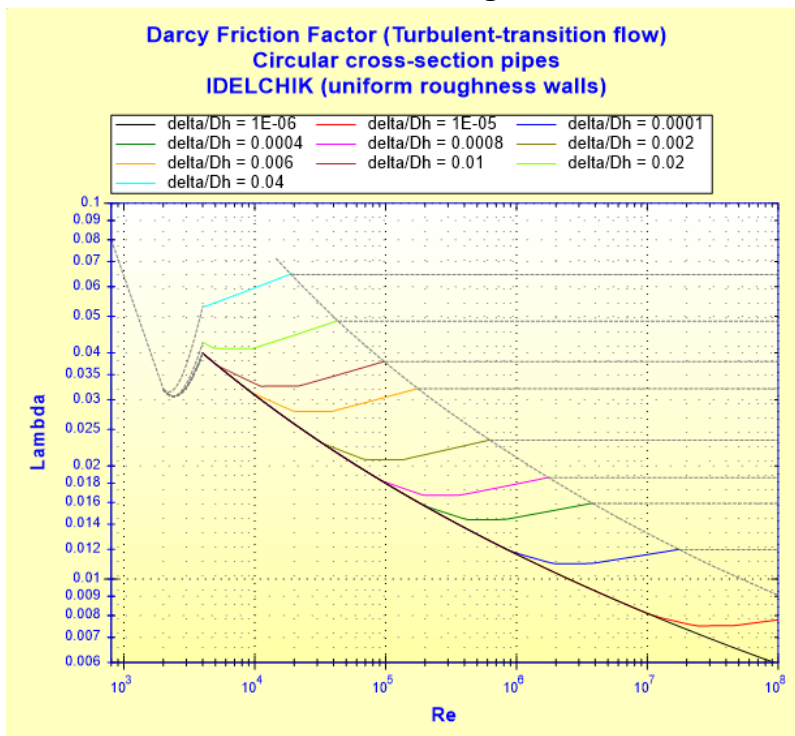
([1] §2.17)

Reynolds number corresponding to the beginning of complete turbulence:

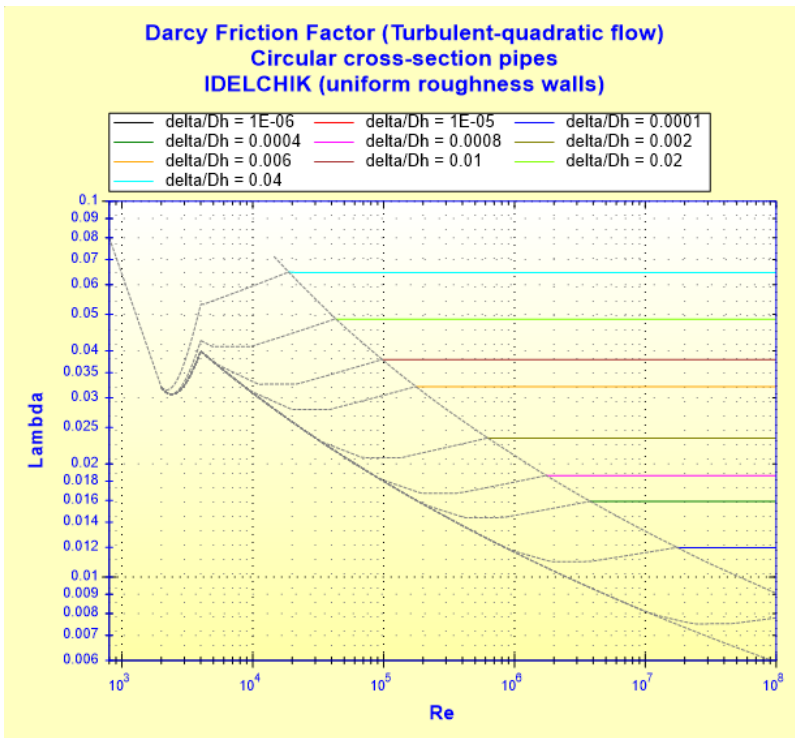
$$\text{Re}''_{\text{lim}} = \frac{217.6 - 382.4 \cdot \log(\bar{\Delta})}{\bar{\Delta}}$$

([1] diagram 2.2)

Transition region



Complete turbulence region



■ critical flow regime ($2000 < Re < 4000$):

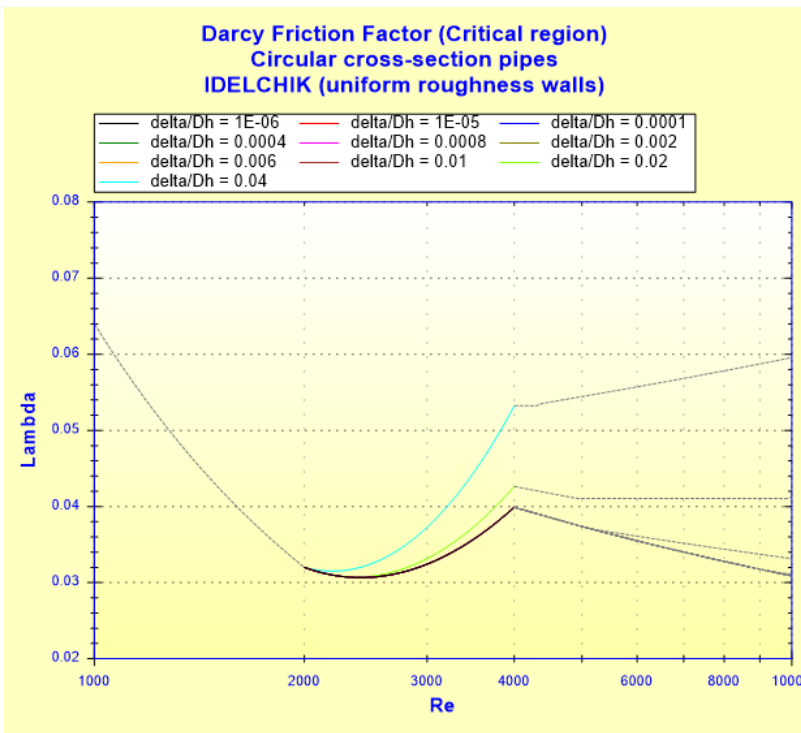
linear interpolation

$$\lambda = \lambda_L \cdot \left(1 - \frac{Re - 2000}{2000}\right) + \lambda_T \cdot \left(\frac{Re - 2000}{2000}\right)$$

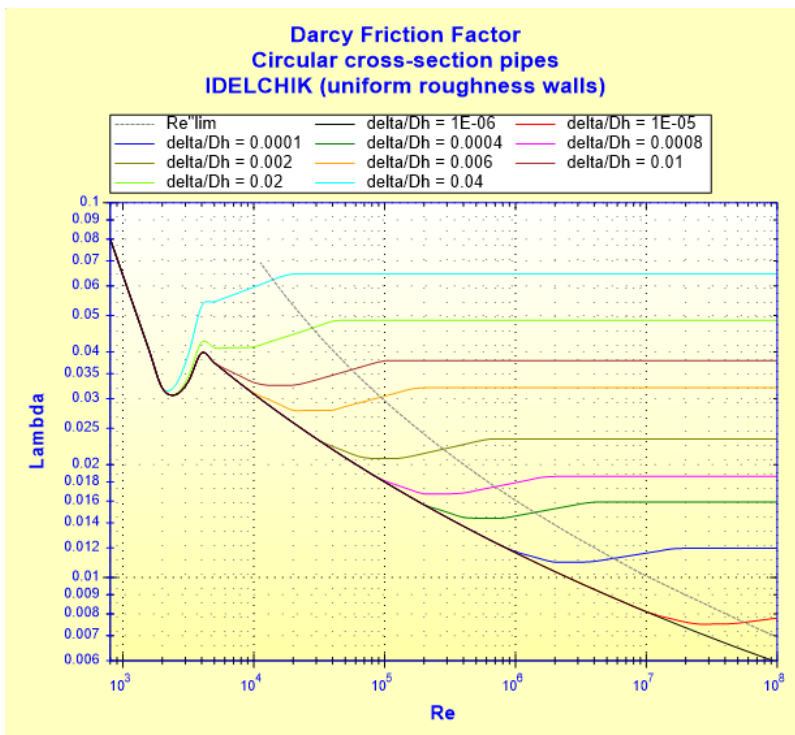
with:

λ_L = laminar friction coefficient obtained with $Re = 2000$

λ_T = turbulent friction coefficient obtained with $Re = 4000$



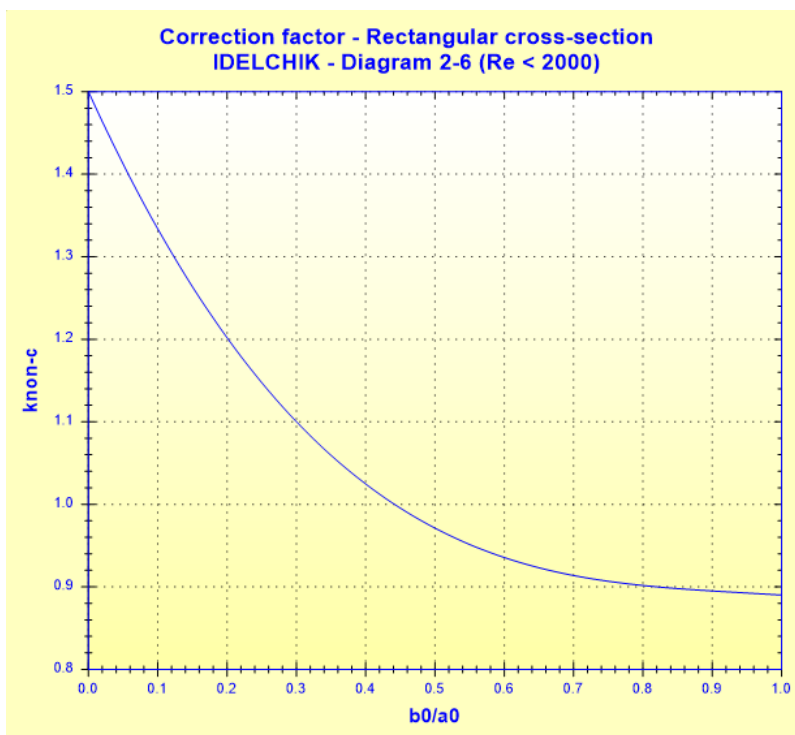
■ all flow regimes:



Correction for Darcy friction factor for noncircular cross-section:

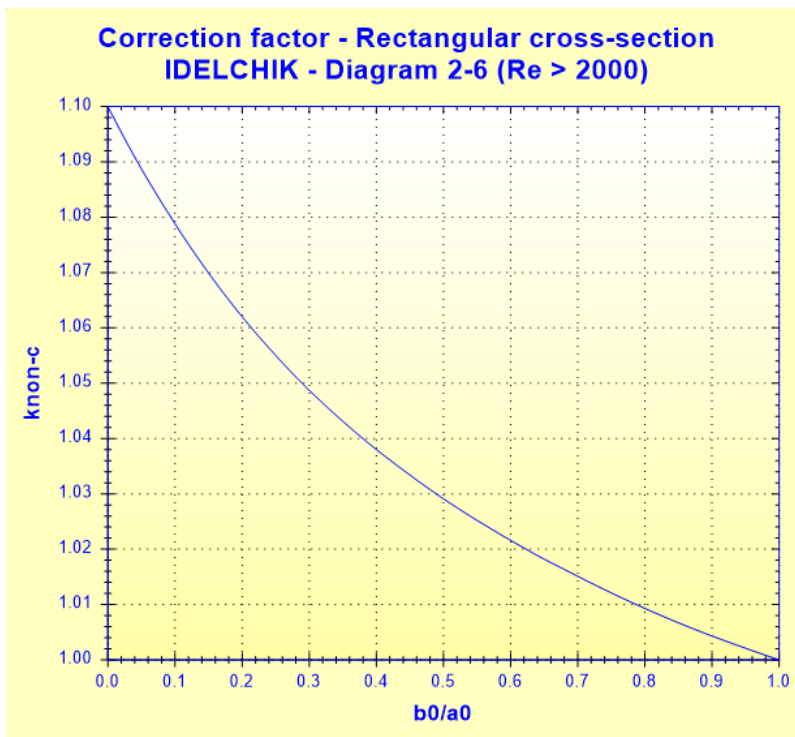
- laminar flow ($Re \leq 2000$):

$$k_{non-c} = f(b_0/a_0) \quad ([1] \text{ diagramme 2.6})$$



- turbulent flow ($Re > 2000$):

$$k_{non-c} = f(b_0/a_0) \quad ([1] \text{ diagramme 2.6})$$



Pressure loss coefficient (based on the mean pipe velocity):

$$\zeta = \lambda \cdot k_{non-c} \cdot \frac{l}{D_h} \quad ([1] \text{ diagram 2.6})$$

Total pressure loss (Pa):

$$\Delta P = \zeta \cdot \frac{\rho \cdot w_0^2}{2} \quad ([1] \text{ diagram 2.6})$$

Total head loss of fluid (m):

$$\Delta H = \zeta \cdot \frac{w_0^2}{2 \cdot g}$$

Hydraulic power loss (W):

$$W_h = \Delta P \cdot Q$$

Symbols, Definitions, SI Units:

a_0	Rectangular cross-section width (m)
b_0	Rectangular cross-section height (m)
D_h	Hydraulic diameter (m)
F_0	Cross-sectional area (m ²)
Q	Volume flow rate (m ³ /s)
G	Mass flow rate (kg/s)
w_0	Mean velocity (m/s)
l	Pipe length (m)
V	Fluid volume in the pipe (m ³)
M	Fluid mass in the pipe (kg)
Re	Reynolds number ()

Re'_{lim}	Limiting Reynolds number for hydraulically smooth law ()
Re''_{lim}	Limiting Reynolds number for quadratic law ()
Δ	Absolute roughness of walls (m)
$\bar{\Delta}$	Relative roughness of walls ()
λ	Darcy friction factor for circular cross-section ()
k_{non-c}	Correction for Darcy friction factor for noncircular cross-section ()
ζ	Pressure loss coefficient (based on the mean pipe velocity) ()
ΔP	Total pressure loss (Pa)
ΔH	Total head loss of fluid (m)
Wh	Hydraulic power loss (W)
ρ	Fluid density (kg/m ³)
ν	Fluid kinematic viscosity (m ² /s)
g	Gravitational acceleration (m/s ²)

Validity range:

- any flow regime: laminar, critical and turbulent ($Re \leq 10^8$)
- $\bar{\Delta} \leq 0.05$
- stabilized flow

Example of application:

The screenshot displays the HydraCalc 2017a software interface. The main window is titled "HydraCalc 2017a - [Straight pipe rectangular cross-section and uniform roughness walls - IDELCHIK (3rd Ed.)]". The interface is divided into several sections:

- Fluid characteristics:**
 - Fluid: Water @ 1 atm [HC]
 - Ref.: IAPWS IF97
 - Temperature: T = 20 °C
 - Pressure: P = 1.013 bar
 - Density: $\rho = 998.2061$ kg/m³
 - Dynamic Viscosity: $\mu = 0.00100159$ N.s/m²
 - Kinematic Viscosity: $\nu = 1.00340E-06$ m²/s
 - Selected: Density
 - Graph: Density (kg/m³) vs Temperature (°C) showing a curve from 1010 to 950 kg/m³ over 100 °C.
- Geometrical characteristics:**
 - Help, Info, Moody Chart, Calculate buttons.
 - 3D model of a rectangular pipe with dimensions: width $a_0 = 0.1$ m, height $b_0 = 0.05$ m, length $l = 1$ m.
 - Flow parameters: $w_0 = 1.0$ m/s (Turbulent), $Q = 0.005$ m³/s, $\Delta = 1.0E-05$ m.
 - Mass flow rate: $\dot{M} = 4.9910$ kg/s.
 - Pressure loss: $\Delta P = 0.001512225$ bar.
 - Head loss: $\Delta H = 0.0154$ m of fluid.
- Complementary results:**

Designation	Symbol	Value	Unit
Hydraulic diameter	D_h	0.06666667	m
Pipe cross-section area	F_0	0.005	m ²
'b ₀ /a ₀ ' ratio	b_0/a_0	0.5	
Internal pipe volume	V	0.005	m ³
Mass of fluid in the pipe	M	4.991031	kg
'Length / Diameter' ratio	l/D_h	15	
Relative roughness	$\bar{\Delta}$	0.00015	
Reynolds number	Re	66440.97	
Friction factor for circular cross-section	λ	0.01962806	
Correction factor for rectangular cross-section	k_{non-c}	1.0291	
Pressure loss per length unit		0.001512225	bar/m
Pressure loss coefficient (based on the mean pipe velocity)	ζ	0.3029885	
Hydraulic power loss	Wh	0.7561123	W

References:

