# Sudden Expansion Circular Cross-Section (Pipe Flow - Guide) 



## Model description:

This model of component calculates the minor head loss (pressure drop) generated by the flow in a sudden expansion.

The head loss by friction in the inlet and outlet piping is not taken into account in this component.

## Model formulation:

Ratio of small to large diameter:

$$
\beta=\frac{d_{1}}{d_{2}}
$$

Minor cross-sectional area $\left(m^{2}\right)$ :

$$
\mathrm{A}_{1}=\pi \cdot \frac{d_{1}^{2}}{4}
$$

Major cross-sectional area $\left(m^{2}\right)$ :

$$
\mathrm{A}_{2}=\pi \cdot \frac{d_{2}^{2}}{4}
$$

Mean velocity in minor diameter ( $\mathrm{m} / \mathrm{s}$ ):

$$
V_{1}=\frac{Q}{A_{1}}
$$

Mean velocity in major diameter ( $\mathrm{m} / \mathrm{s}$ ):

$$
V_{2}=\frac{Q}{A_{2}}
$$

Reynolds number in minor diameter:

$$
N_{\mathrm{Re}_{1}}=\frac{V_{1} \cdot d_{1}}{v}
$$

Reynolds number in major diameter:

$$
N_{\mathrm{Re}_{2}}=\frac{V_{2} \cdot d_{2}}{v}
$$

Local resistance coefficient ( $\operatorname{Re}_{1} \geq 10^{4}$ ):

$$
K_{1}=\left(1-\beta^{2}\right)^{2} \quad \text { ([1] equation 11.6) (Borda-Carnot equation) }
$$



Total pressure loss coefficient (based on mean velocity in minor diameter):

$$
K=K_{1}
$$

Total pressure loss (Pa):

$$
\Delta P=K \cdot \frac{\rho_{m} \cdot V_{1}^{2}}{2}
$$

Total head loss of fluid ( $m$ ):

$$
\Delta H=K \cdot \frac{V_{1}^{2}}{2 \cdot g}
$$

Hydraulic power loss (W):

$$
W h=\Delta P \cdot Q
$$

Symbols, Definitions, SI Units:
$d_{1} \quad$ Minor diameter ( $m$ )
$\mathrm{d}_{2} \quad$ Major diameter ( $m$ )
$\beta \quad$ Ratio of small to large diameter ()
$A_{1} \quad$ Minor cross-sectional area ( $m^{2}$ )
$A_{2} \quad$ Major cross-sectional area $\left(m^{2}\right)$
Q Volume flow rate ( $\mathrm{m}^{3} / \mathrm{s}$ )
$G \quad$ Mass flow rate ( $\mathrm{kg} / \mathrm{s}$ )
$V_{1} \quad$ Mean velocity in minor diameter ( $\mathrm{m} / \mathrm{s}$ )
$V_{2} \quad$ Mean velocity in major diameter ( $\mathrm{m} / \mathrm{s}$ )
$\mathrm{NRe}_{1} \quad$ Reynolds number in minor diameter ()
$\mathrm{NRe}_{2}$ Reynolds number in major diameter ()
$\mathrm{K}_{1} \quad$ Local resistance coefficient ()
K Total pressure loss coefficient (based on mean velocity in minor diameter) ()
$\Delta \mathrm{P} \quad$ Total pressure loss ( Pa )
$\Delta H \quad$ Total head loss of fluid (m)
Wh Hydraulic power loss (W)
$\rho_{m} \quad$ Fluid density ( $\mathrm{kg} / \mathrm{m}^{3}$ )
$v \quad$ Fluid kinematic viscosity ( $\mathrm{m}^{2} / \mathrm{s}$ )
$9 \quad$ Gravitational acceleration $\left(\mathrm{m} / \mathrm{s}^{2}\right)$

## Validity range:

- turbulent flow regime in minor diameter $\left(\mathrm{NRe}_{1} \geq 10^{4}\right)$


## Example of application:



Fluid characteristics
Fluid: Water @ $1 \mathrm{~atm}[\mathrm{HC}]$ Ref.: IAPWS IF97
 Kinematic Viscosity : V 1.00340E-06 $\mathrm{m}^{2} / \mathrm{s}$




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Geometrical characteristics
Help Info
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$\Delta H \quad 0.2333 \mathrm{~m}$ of fluid
Complementary results

| Designation | Symbol | Value | Unit |
| :---: | :---: | :---: | :---: |
| Diameters ratio ( $\mathrm{d} 1 / \mathrm{d} 2$ ) | $\beta$ | 0.6130868 |  |
| Minor diameter cross-section area | A1 | 0.001458963 | $\mathrm{m}^{2}$ |
| Major diameter cross-section area | A2 | 0.003881508 | $\mathrm{m}^{2}$ |
| Cross-sections area ratio | A1/A2 | 0.3758754 |  |
| Minor diameter Reynolds number | NRe1 | 147207.5 |  |
| Major diameter Reynolds number | NRe2 | 90251 |  |
| Coefficient of local resistance (Equation 11.6) | K1 | 0.3895316 |  |
| Pressure loss coefficient (based on velocity in minor diameter) | K | 0.3895316 |  |
| Hydraulic power loss | Wh | 11.41705 | w |
|  |  |  |  |
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|  |  |  |  |
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## References:

[1] Pipe Flow: A Practical and Comprehensive Guide. Donald C. Rennels and Hobart M. Hudson. (2012)

## HydrauCalc

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